



Course Title: Algorithms and Data Structure
Date: Aug. 29, 2018 (Final Exam)

Course Code: CSE 152
Allowed time: 2 hrs

Total Marks: 50 Marks
No. of Pages: (2)

Welcome to the final Exam for *Algorithms and Data Structure*. Read each problem carefully. There are five required problems (ordered as course syllabus sequence - each worth 10 points- Extra 10 points). Please use a separate sheet for the answer to each question. Assume any missing data. Good luck and be sure to show your work!

QUESTION NO. (1) (10 MARKS) [INTRODUCING DATA STRUCTURES AND ALGORITHMS]

Q1-A) What is a Data Structure? What are the advantages and disadvantages of the various data-structures? 5

Q1-B) What is an algorithm? Give some practical examples of using Algorithms. List the major steps for developing an algorithm. 3

Q1-C) What are the criteria of algorithm analysis? What is meant by time and space complexity of algorithm? 2

Q1-D) What is meant by Data abstraction and ADT? What data structure implements LIFO behaviour? 2

QUESTION NO. (2) (10 MARKS) [STRING-LISTS-TUPLES-DICTIONARY]

Q2-A) List the different operations (at least three) which can be performed on (String-Lists-tuples-Dictionary). 3

Q2-B) Write a Python program to multiplies all the items in a list. 2

Q2-C) Write a Python program to find maximum and the minimum value in a set. 2

Q2-D) Write a Python program to sort (ascending and descending) a dictionary by value. 3

QUESTION NO. (3) (10 MARKS) [ARRAYS]

Q3-A) What are the Similarities and differences between the array and the list? 2

Q3-B) Define one-dimensional array and two-dimensional array. 2

Q3-C) What are Modules? Why we use Modules in python? What is the ctypes and NumPy Module. 3

Q3-D) Write a Python program to reverse the order of the items in the array. 3

QUESTION NO. (4) (10 MARKS) [ALGORITHM ANALYSIS]

Q4-A) What is the difference between Algorithms – Code – Pseudocode? 3

Q4-B) Evaluate the complexity following Python Code:

```
def ex1( n ):  
    total = 0  
    for i in range( n ) :  
        total += i  
    return total
```

```
def ex3( n ):  
    count = 0  
    for i in range( n ) :  
        for j in range( n ) :  
            count += 1  
    return count
```

3

Q4-C) For each function $f(n)$ below, give an asymptotic upper bound using "big-Oh" notation. You should give the tightest bound possible.

- a) $f(n) = 100n^3 - 7n^3 + 14n^2$
- b) $f(n) = 100n^3 - 100n^3 + 7n^2$
- c) $f(n) = \log(7n^2)$

4

QUESTION NO. (5) (20 MARKS) (DYNAMIC DATA STRUCTURES)

Q5-A) Write the Pseudocode Add (value) for the Singly Linked List. 4

Q5-B) We can implement each of the stack operations with just a few lines of code. Write the Pseudocode for $STACK-EMPTY(S)$, $PUSH(S,x)$, $Pop(S,x)$. 4

Q5-C) Suppose q is an instance of the Queue class and assume that the array implementation is used. Also, assume the size of the array is 5. Show q after all of the following operations have been completed. Assume the queue is empty to start with. Show how the front, rear, and elements change. 4

(i) $q.enqueue(39)$; (ii) $q.enqueue(22)$; (iii) $item1 = q.dequeue()$; (iv) $q.enqueue(59)$; (v) $item2 = q.dequeue()$; (vi) $item3 = q.dequeue()$

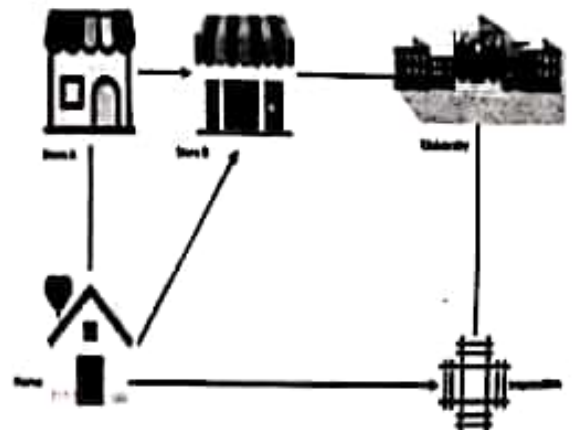
Q5-D) Show the stack elements after the following operations have all been completed (Draw the final picture of $s.elements[]$ and show the value of $s.top$). 4

(i) $s.push(20)$; (ii) $s.push(51)$; (iii) $s.pop()$; (iv) $s.push(43)$.

Q5-E) What is the difference between Queue and Priority Queue? 2

Q5-F) For the following figure: 2

- List two data structures to implement a map.
- Write the steps to find the shortest path from home to the university.
- What is the relation between data structure and the algorithm used to find the shortest path from home to the university?





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Model Answer

QUESTION NO. (1) (10 MARKS) [INTRODUCING DATA STRUCTURES AND ALGORITHMS]

Q1-A) What is a Data Structure? What are the advantages and disadvantages of the various data-structures?

- A data structure is an arrangement of data in a computer's memory (or sometimes on a disk).
- A group of data elements grouped together under one name. These data elements, known as members, can have different types and different lengths.

Data Structure	Advantages	Disadvantages
Array	Quick insertion, very fast access if index known.	Slow search, slow deletion, fixed size.
Ordered array	Quicker search than unsorted array.	Slow insertion and deletion, fixed size.
Stack	Provides last-in, first-out access.	Slow access to other items.
Queue	Provides first-in, first-out access.	Slow access to other items.

Q1-B) What is an algorithm? Give some practical examples of using Algorithms. List the major steps for developing an algorithm.

- Algorithm: Step-by-step procedure for performing some task in a finite amount of time.
- Some practical examples of using Algorithms: Search Engines - GPS navigation
Self-Driving Cars - E-commerce - Banking - Medical diagnosis- Robotics
- The major steps for developing an algorithm.
 - Design the algorithm: correctness and efficiency
 - Verify and prove correctness :will it work for all cases?
 - Analyze the algorithm: how long will it run?
 - Implement the algorithm: coding and programming

Q1-C) What are the criteria of algorithm analysis? What is meant by time and space complexity of algorithm?

- An algorithm is said to be efficient and fast, if it takes less time to execute and consumes less memory space.
- The performance of an algorithm is measured on the basis of following properties :
 1. Time Complexity: how long will it run?
 2. Space Complexity: how memory and CPU will it use?

Q1-D) What is meant by Data abstraction and ADT? What data structure implements LIFO behaviour?

- An abstraction is a mechanism for separating the properties of an object and restricting the focus to those relevant in the current context.
- Data abstraction is the separation of the properties of a data type (its values and operations) from the implementation of that data type.
- An abstract data type (or ADT) is a programmer-defined data type that specifies a set of data values and a collection of well-defined operations that can be performed on those values.
- Stack

QUESTION NO. (2) (10 MARKS) [STRING-LISTS-TUPLES-DICTIONARY]

Q2-A) List the different operations (at least three) which can be performed on (String-Lists-tuples-Dictionary).

<u>Data structure</u>	<u>Operations</u>
String	<u>Slicing – Concatenation - In and Not In</u>
Lists	<div style="border: 1px solid black; padding: 5px;"> <pre> items.append(x) Add item x to the end of items. items.insert(i, x) Insert item x into items at index i. items.pop() Remove and return the last item in items. items.pop(i) Remove and return items[i]. items.remove(x) Remove item x from items. Raises ValueError when x not in items. items.reverse() Reverse the order of the elements in items. items.sort() Sort the list items. </pre> </div>
Dictionary	<ul style="list-style-type: none"> ➤ <u>len(my_dict)</u> ➤ <u>element in my_dict</u> ➤ <u>my_dict.copy</u>
tuples	<ul style="list-style-type: none"> • <u>left hand side assignment - - In and Not In - Concatenation</u>

Q2-B) Write a Python program to multiplies all the items in a list.

```
list1=[3,1,2,3]
mul=1
for x in list1:
    mul *= x
print ('mul= ', mul)
```



Q2-C) Write a Python program to find maximum and the minimum value in a set.

#Create a set

```
setA = set([5, 10, 3, 15, 2, 20])
```

#Find maximum value

```
print(max(setA))
```

#Find minimum value

```
print(min(setA))
```

Q2-D) Write a Python program to sort (ascending and descending) a dictionary by value.

```
import operator
```

```
d = {1: 2, 3: 4, 4: 3, 2: 1, 0: 0}
```

```
print('Original dictionary : ',d)
```

```
sorted_d = sorted(d.items(), key=operator.itemgetter(0))
```

```
print('Dictionary in ascending order by value : ',sorted_d)
```

```
sorted_d = sorted(d.items(), key=operator.itemgetter(0),reverse=True)
```

```
print('Dictionary in descending order by value : ',sorted_d)
```

QUESTION NO. (3) (10 MARKS) [ARRAYS]

Q3-A) What are the Similarities and differences between the array and the list?

- **Similarities:** The two structures are both sequences that are composed of multiple sequential elements that can be accessed by position.
- **Differences:**
 - An array has a limited number of operations. which commonly include those for array creation, reading a value from a specific element, and writing a value to a specific element.
 - The list, on the other hand, provides a large number of operations for working with the contents of the list.

- ➡ The list can grow and shrink during execution as elements are added or removed while the size of an array cannot be changed after it has been created.
- ➡ List is an array of pointers to python objects.

Arrays	Lists
Best suited for problems requiring a sequence in which the maximum number of elements are known up front.	is the better choice when <u>the size of the sequence needs to change after it has been created.</u>
Use less memory	contains <u>more storage space</u> than is needed to store the items currently in the list (twice the necessary capacity).
Faster execution	Allows for quick and easy expansion as new items are added to the list.

Q3-B) Define one-dimensional array and two-dimensional array.

One-dimensional array is a collection of contiguous elements in which individual elements are identified by a unique integer subscript starting with zero. Once an array is created, its size cannot be changed.

A **two-dimensional array** consists of a collection of elements organized into rows and columns. Individual elements are referenced by specifying the specific row and column indices (r, c), both of which start at 0.

Q3-C) What are Modules? Why we use Modules in python? What is the ctypes and NumPy Module.

- ➡ Modules are files containing Python definitions and statements (ex. *name.py*)

1. Facilitate python programs in achieving complex functions.
2. Simplicity.
3. Maintainability.
4. Code Reusability.
5. Popularity.

NumPy: Similar to Numeric, but handles arrays slightly differently and has a few other built-in commands and functions.

- ➡ **The ctypes Module:** This module provides access to the diverse set of data types available in the C language and the complete functionality provided by a wide range of C libraries. The ctypes module provides the capability to create hardware-

supported arrays just like the ones used to implement Python's string, list, tuple, and dictionary collection types.

Q3-D) Write a Python program to reverse the order of the items in the array.

```
from array import *
array_num = array('i', [1, 3, 5, 3, 7, 1, 9, 3])
print("Original array: "+str(array_num))
array_num.reverse()
print("Reverse the order of the items:")
print(str(array_num))
```

QUESTION NO. (4) (10 MARKS) [ALGORITHM ANALYSIS]

Q4-A) What is the difference between Algorithms – Code – Pseudocode?

- An algorithm is a step-by-step procedure which, starting with an input instance, produces a suitable output.
- In contrast, *code* is an implementation of an algorithm that can be executed by a computer.
- Pseudocode lies between these two.

Q4-B) Evaluate the complexity following Python Code:

```
def ex1( n ):
    total = 0
    for i in range( n ) :
        total += i
    return total
```

$O(n)$

```
def ex3( n ):
    count = 0
    for i in range( n ) :
        for j in range( n ) :
            count += 1
    return count
```

$O(n^2)$

Q4-C) For each function $f(n)$ below, give an asymptotic upper bound using "big-Oh" notation. You should give the tightest bound possible.

- a) $f(n) = 100n^3 - 7n^3 + 14n^2$
- b) $f(n) = 100n^3 - 100n^3 + 7n^2$
- c) $f(n) = \log(7n^2)$
- a) $O(n^1)$ b) $O(n^2)$ c) $O(\log(n))$

QUESTION NO. (5) (20 MARKS) (DYNAMIC DATA STRUCTURES)

Q5-A) Write the Pseudocode Add (value) for the Singly Linked List.

```
1) algorithm Add(value)
2)   Pre: value is the value to add to the list
3)   Post: value has been placed at the tail of the list
4)   n ← node(value)
5)   if head = 0
6)     head ← n
7)     tail ← n
8)   else
9)     tail.Next ← n
10)    tail ← n
11)  end if
12) end Add
```

Q5-B) We can implement each of the stack operations with just a few lines of code. Write the Pseudocode for *STACK-EMPTY(S)*, *PUSH(S,x)*, *Pop(S,x)*.

STACK-EMPTY(S)

```
1 if S.top == 0
2   return TRUE
3 else return FALSE
```

PUSH(S,x)

```
1 S.top = S.top + 1
2 S[S.top] = x
```

POP(S)

```
1 if STACK-EMPTY(S)
2   error "underflow"
3 else S.top = S.top - 1
4   return S[S.top + 1]
```

Q5-C) Suppose *q* is an instance of the Queue class and assume that the array implementation is used. Also, assume the size of the array is 5. Show *q* after all of the following operations have been completed. Assume the queue is empty to start with. Show how the front, rear, and elements change.

(i) *q.enqueue(39)*; (ii) *q.enqueue(22)*; (iii) *item1 = q.dequeue()*; (iv) *q.enqueue(59)*; (v) *item2 = q.dequeue()*; (vi) *item3 = q.dequeue()*

operation	front	rear	elements change
<i>q.enqueue(39)</i>	39	39	39
<i>q.enqueue(22)</i>	39	22	39,22
<i>item1 = q.dequeue()</i>	22	22	item1 = 39
<i>q.enqueue(59)</i>	22	59	22,59
<i>item2 = q.dequeue()</i>	59	59	item2 = 22
<i>item3 = q.dequeue()</i>	Null	Null	item3 = 59

Q5-D) Show the stack elements after the following operations have all been completed (Draw the final picture of s.elements[] and show the value of s.top).

(i) s.push (20); (ii) s.push (51); (iii) s.pop(); (iv) s.push (-43).

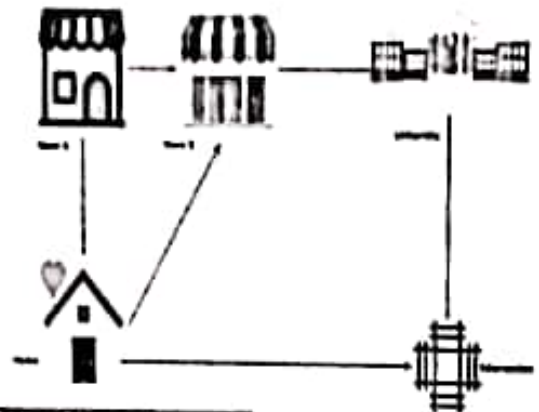
operation	Stack elements	TOS
s.push (20)	20	20
s.push (51)	20,51	51
s.pop();	20	20
s.push (-43).	20,43	43

Q5-E) What is the difference between Queue and Priority Queue?

- ◆ A regular queue is a first-in and first-out data structure. Elements are appended to the end of the queue and are removed from the beginning of the queue.
- ◆ In a priority queue, elements are assigned with priorities.
- ◆ When accessing elements, the element with the highest priority is removed first.

Q5-F) For the following figure:

- List two data structures to implement a map.
- Write the steps to find the shortest path from home to the university.
- What is the relation between data structure and the algorithm used to find the shortest path from home to the university?



Home	(49.2, -123.4)
Store A	(49.3, -123.4)
Store B	(49.3, -123.3)
School	(49.3, -123.2)
Intersection	(49.2, -123.2)

Array

(Home, Store A)
(Store A, Home)
(Store A, Store B)
(Home, Intersection)
(Store A, Store B)
(Store A, School)
(School, Store B)
(School, Intersection)
(Intersection, School)

**Hash
table
or
MAP**

Home	(Store A, Store B, Intersection)
Store A	(Home, Store B)
Store B	(School)
School	(Store B, Intersection)
Intersection	(School)

- Find places you can go from home
- From each of those places, find all paths
- Keep track of the distance you've traveled as you go
- Repeat this process until you get to school
- Compare the distance you've traveled
- Find the shortest path

- ◆ **Algorithms** manipulate the data in these structures in various ways, such as: Inserting a new data item, Searching for a particular item, and Sorting the items.
- ◆ **Using hash table or map in this case will be faster than using a list or array.**