



Please Answer ALL the Questions. Ensure your answer is well organized and written clearly to guarantee your mark.

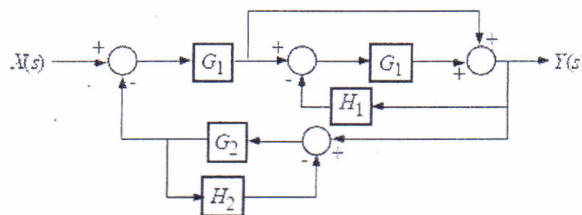
1. (15 Min - 6 points) Find the solution to the differential equation:

$$\ddot{x} + 4\dot{x} + 5x = 10e^t \quad \text{where} \quad x(0) = 1, \quad \dot{x}(0) = 2$$

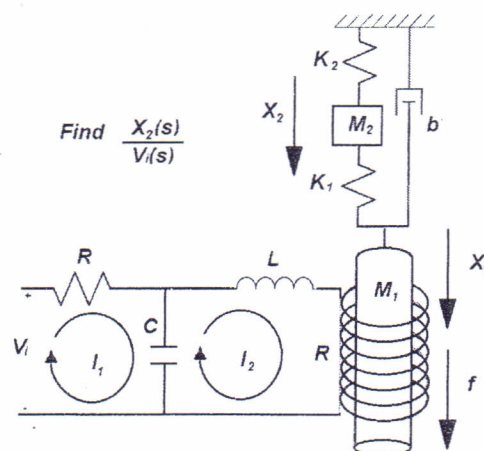
2. (10 Min - 8 points) Complete the following statements:

- There are two modes of control to the DC Motor. They are — and —.
- In the — control of a DC motor, the — current is constant.
- The flux is proportional to — and the torque is proportional to — and — while the back EMF is proportional to —.
- Plot the equivalent circuit to your answer in (b).
- The main advantage of closed loop system over open loop system are — and — while the disadvantages are — and —. However, the open loop system advantages are — and —.

3. (20 Min - 8 points) Find  $\frac{Y(s)}{X(s)}$  using block diagram reduction



4. (15 Min - 6 points) Find  $\frac{x_2(s)}{v_i(s)}$ . Ignore any back EMF



5. (30 Min - 10 points) Find the Root Locus of the following Open Loop Transfer Function showing details of each step.

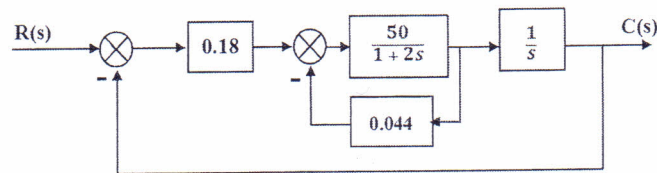
$$G(s) = \frac{1}{s(s+1)(s+2)(s+3)}$$

6. (15 Min - 6 points) For the following closed loop system:

$$T(s) = \frac{5}{s^5 + 5s^4 + 11s^3 + 23s^2 + 28s + 12}$$

- (a) Find The roots location
- (b) Determine the stability of the system

7. (15 Min - 6 points) For the following system, find:



- (a) The damping ratio  $\zeta$
- (b) The natural frequency  $\omega_n$
- (c) The maximum overshoot  $M_p$
- (d) The peak time  $t_p$
- (e) The rising time  $t_r$
- (f) The settling time  $t_s$  for the 2% error.

Good Luck...

Dr. John FW Zaki