

Mansoura University Faculty of Engineering Dept. of Power Mech. Eng. Course Title: 3D Modeling & Simulation of Heat Transfer & Fluid Flow Course Code: MPE371		BME Level 300 January 2019 Exam Type: Final Time: 2 Hours Full Mark: 50
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Attempt All Five Questions. Assume Any Missing Data. Questions Are Equal Weight But Are Not Equal Difficulty.

Question (1)

- Mention the names of three conservation laws.
- Write an example for ordinary differential equation (ODE) in fluid mechanics.
- Write the Fourier's law of heat conduction. Why do we put the negative sign in the Fourier's law of heat conduction? When does the heat flux (q) equal zero?
- For one-dimensional transient (unsteady) heat conduction, what is the type of this partial differential equation (PDE)? Why? What are the name & units of property (α) in this equation?

Question (2)

- An incompressible steady-flow pattern is given by $u = x^3 + 2z^2$ and $w = y^3 - 2yz$. What is the most general form of the third component, $v(x, y, z)$, which satisfies continuity?
- Mention the names of different forces in the momentum equation.
- When does the gravitational force has a value in the momentum equation? When is this value positive? When is this value negative?

Question (3)

For the following velocity distribution.

$$u/U_{\infty} = a + b\eta + c\eta^2 + d\eta^3$$

Where a, b, c, d are constants and $\eta = y/\delta$

- Write the four boundary conditions required to determine the constants a, b, c, d.
- By solving these four equations, obtain the values of constants a, b, c, d.
- Calculate the displacement thickness (δ^*) and momentum thickness (θ) in terms of δ .

Question (4)

4.a Consider the steady-state two-dimensional heat conduction. Show that the steady-state temperature distribution on a heated plate can be modeled using the equation

$$\frac{\partial^2 T}{\partial x^2} + \frac{\partial^2 T}{\partial y^2} = 0$$

For the square grid ($\Delta x = \Delta y$) and using the approximation of $\partial^2 T / \partial x^2$ and $\partial^2 T / \partial y^2$, show that the above equation can be written as

$$T_{i+1,j} + T_{i-1,j} + T_{i,j+1} + T_{i,j-1} - 4T_{i,j} = 0$$

4.b What is the difference between Laplace equation & Poisson equation? What is the type of these partial differential equations (PDEs)? Why?

Question (5)

Consider the problem of heat conduction with uniform heat generation (q) in a rod whose ends are maintained at constant temperatures of $T_0 = 100^\circ\text{C}$ and $T_5 = 200^\circ\text{C}$ respectively. The one-dimensional problem is governed

$$\frac{d}{dx} \left(k \frac{dT}{dx} \right) + q = 0$$

Take rod length L equals 2 cm, thermal conductivity k equals 0.5 W/m.K, heat generation q equals 10^6 W/m^3 , cross-sectional area A is 1 m^2 , $\delta x = 0.5 \text{ cm}$.

i. Integrate the above equation 2 times with respect to x . Use the 2 boundary conditions at rod ends to obtain the values of the constants C_1 & C_2 . Use this temperature distribution equation to obtain the values of the temperature T_1, T_2, T_3, T_4 at $x = 2.5, 7.5, 12.5, 17.5 \text{ mm}$ respectively.

ii. Using the control volume method, obtain the discretised equation for nodal points 2 and 3, the discretised equation for nodal point 1, and the discretised equation for nodal point 4.

Good Luck
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